

# Filter-enhanced MLP is All You Need for Sequential Recommendation

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Code: <https://github.com/RUCAIBox/FMLP-Rec>.

Dataset: Beauty Sports Toys Yelp Nowplaying Retailrocket Tmall Yoochoose



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# Motivation & Solution

## **Motivation (Take SASRec as an example):**

- logged user behavior data is inevitable to contain noise
- and deep recommendation models are easy to overfit on these logged data

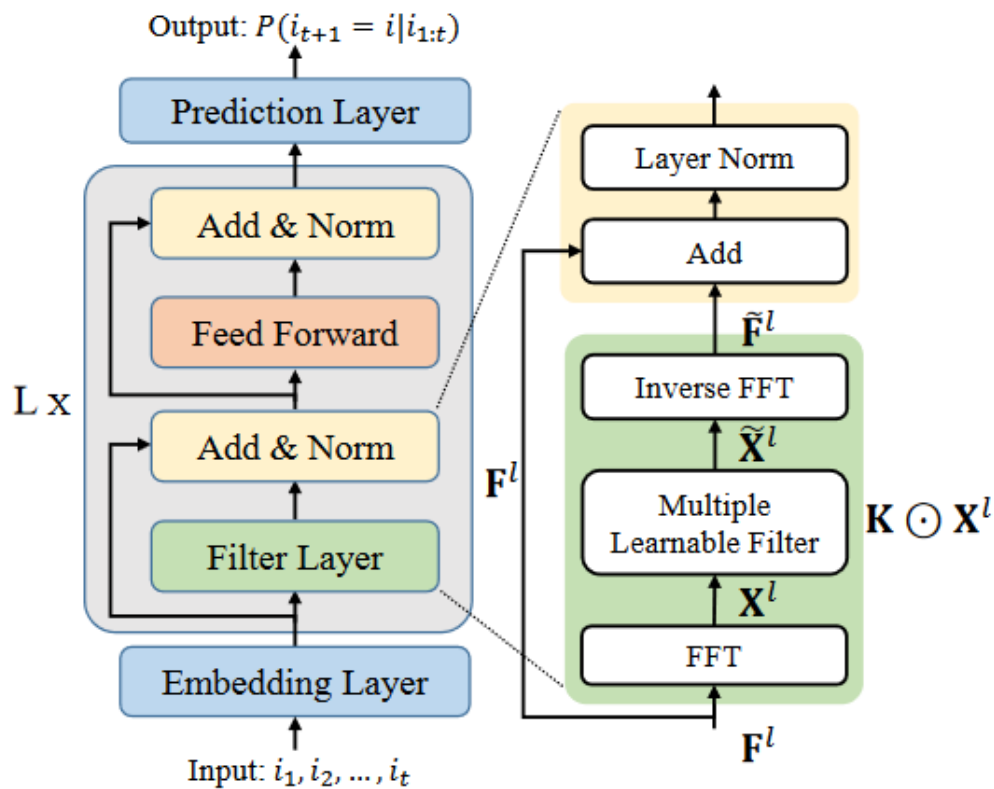
## **Solution (Take SASRec as an example) :**

To tackle this problem, we borrow the idea of filtering algorithms from signal processing that attenuates the noise in the frequency domain

By replacing the self-attention components from Transformers to a novel filter layer

In a filter we perform Fast Fourier Transform (FFT) to convert the input representations into the frequency domain and an inverse FFT procedure recovers the denoised representations.

# Problem Statement



Assume that we have a set of users and items, denoted by  $\mathcal{U}$  and  $\mathcal{I}$ , respectively, where  $u \in \mathcal{U}$  denotes a user and  $i \in \mathcal{I}$  denotes an item. The numbers of users and items are denoted as  $|\mathcal{U}|$  and  $|\mathcal{I}|$ , respectively. For sequential recommendation with implicit feedback, a user  $u$  has a context  $c$ , a chronologically-ordered interaction sequence with items:  $c = \{i_1, \dots, i_n\}$ , where  $n$  is the number of interactions and  $i_t$  is the  $t$ -th item that the user  $u$  has interacted with. For convenience, we use  $i_{j:k}$  to denote the subsequence, i.e.,  $i_{j:k} = \{i_j, \dots, i_k\}$  where  $1 \leq j < k \leq n$ .

Based on the above notations, we now define the task of sequential recommendation. Formally, given the contextual item sequence of a user  $c = \{i_1, \dots, i_n\}$ , the task of sequential recommendation is to predict the next item that the user is likely to interact with at the  $(n + 1)$ -th step, denoted as  $p(i_{n+1} | i_{1:n})$ .

Figure 2: The overview of our FMLP-Rec, an all-MLP model that stacks multiple learnable filter-enhanced blocks.

# Method

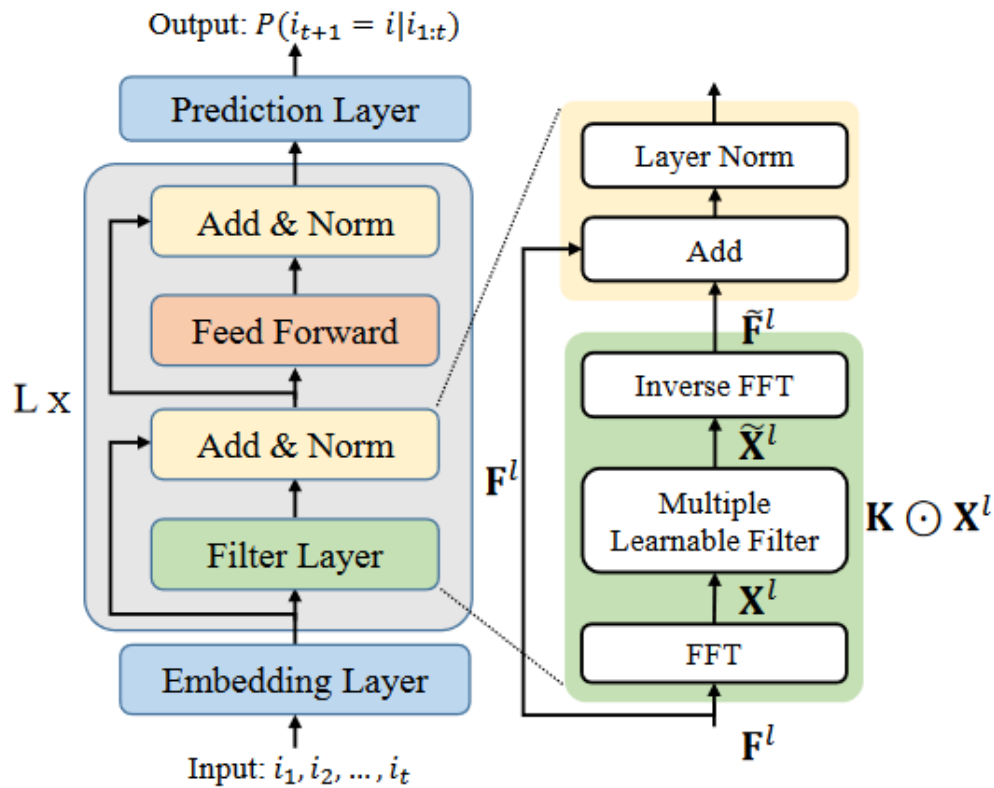


Figure 2: The overview of our FMLP-Rec, an all-MLP model that stacks multiple learnable filter-enhanced blocks.

$$X_k = \sum_{n=0}^{N-1} x_n e^{-\frac{2\pi i}{N} nk}, \quad 0 \leq k \leq N-1. \quad (1)$$

$$x_n = \frac{1}{N} \sum_{k=0}^{N-1} X_k e^{\frac{2\pi i}{N} nk}. \quad (2)$$

$$E_l = \text{Dropout}(\text{LayerNorm}(E + P)). \quad (3)$$

$$X^l = \mathcal{F}(F^l) \in \mathbb{C}^{n \times d} \quad (4)$$

$$\tilde{X}^l = W \odot X^l, \quad (5)$$

$$\tilde{F}^l \leftarrow \mathcal{F}^{-1}(\tilde{X}^l) \in \mathbb{R}^{n \times d}. \quad (6)$$

$$\tilde{F}^l = \text{LayerNorm}(F^l + \text{Dropout}(\tilde{F}^l)) \quad (7)$$

$$\text{FFN}(\tilde{F}^l) = (\text{ReLU}(\tilde{F}^l W_1 + b_1)) W_2 + b_2, \quad (8)$$

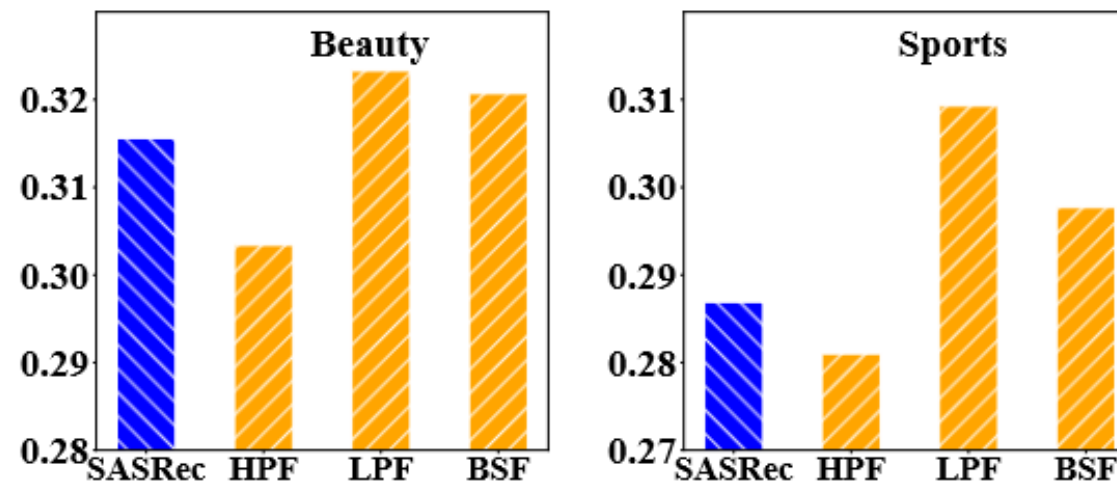
$$P(i_{t+1} = i | i_{1:t}) = e_i^\top F_t^l,$$

$$L = - \sum_{u \in \mathcal{U}} \sum_{t=1}^n \log \sigma \left( P(i_{t+1} | i_{1:t}) - P(i_{t+1}^- | i_{1:t}) \right), \quad (10)$$

# Experiments

**Table 1: Performance comparison of SASRec and GRU4Rec with different filtering algorithms.**

| Methods | Filter | Beauty        |               | Sports        |               |
|---------|--------|---------------|---------------|---------------|---------------|
|         |        | HR@10         | NDCG@10       | HR@10         | NDCG@10       |
| GRU4Rec |        | 0.4106        | 0.2584        | 0.4299        | 0.2527        |
|         | +HPF   | 0.3828        | 0.2228        | 0.3654        | 0.2063        |
|         | +LPF   | 0.4351        | <b>0.2689</b> | <b>0.4481</b> | <b>0.2578</b> |
|         | +BSF   | <b>0.4372</b> | 0.2658        | 0.4432        | 0.2563        |
| SASRec  |        | 0.4696        | 0.3156        | 0.4622        | 0.2869        |
|         | +HPF   | 0.4544        | 0.3037        | 0.4530        | 0.2785        |
|         | +LPF   | 0.4941        | 0.3320        | 0.5040        | 0.3138        |
|         | +BSF   | <b>0.5011</b> | <b>0.3334</b> | <b>0.5115</b> | <b>0.3172</b> |



**Figure 1: Performance (NDCG@10) comparison of all-MLP variants of SASRec with different filtering algorithms.**

# Experiments

**Table 2: Time complexity and receptive field of the proposed FMLP-Rec with Caser and SASRec, where  $n$  and  $k$  denote the sequence length and convolution kernel size, respectively. For simplicity, we omit other same terms (e.g., hidden size) and highlight the difference at the sequence level.**

|          | Time Complexity per Layer | Receptive Field |
|----------|---------------------------|-----------------|
| Caser    | $O(kn)$                   | $k$             |
| SASRec   | $O(n^2)$                  | $n$             |
| FMLP-Rec | $O(n \log n)$             | $n$             |

**Table 3: Statistics of the datasets after preprocessing.**

| Dataset      | # Sequences | # Items | # Actions | # Sparsity |
|--------------|-------------|---------|-----------|------------|
| Beauty       | 22,363      | 12,101  | 198,502   | 99.93%     |
| Sports       | 25,598      | 18,357  | 296,337   | 99.95%     |
| Toys         | 19,412      | 11,924  | 167,597   | 99.93%     |
| Yelp         | 30,431      | 20,033  | 316,354   | 99.95%     |
| Nowplaying   | 145,612     | 59,593  | 1,085,410 | 99.99%     |
| Retailrocket | 321,032     | 51,428  | 871,637   | 99.99%     |
| Tmall        | 66,909      | 37,367  | 427,797   | 99.98%     |
| Yoochoose    | 470,477     | 19,690  | 1,434,349 | 99.98%     |

# Experiments

**Table 4: Performance comparison of different methods on four datasets containing user transaction records. The best performance and the second best performance methods are denoted in bold and underlined fonts respectively.**

| Datasets | Metric  | PopRec | FM     | AutoInt | GRU4Rec | Caser  | HGN    | RepeatNet | CLEA   | SASRec        | BERT4Rec      | SRGNN  | GCSAN         | FMLP-Rec      |
|----------|---------|--------|--------|---------|---------|--------|--------|-----------|--------|---------------|---------------|--------|---------------|---------------|
| Beauty   | HR@1    | 0.0678 | 0.0405 | 0.0447  | 0.1337  | 0.1337 | 0.1683 | 0.1578    | 0.1325 | 0.1870        | 0.1531        | 0.1729 | <u>0.1973</u> | <b>0.2011</b> |
|          | HR@5    | 0.2105 | 0.1461 | 0.1705  | 0.3125  | 0.3032 | 0.3544 | 0.3268    | 0.3305 | <u>0.3741</u> | 0.3640        | 0.3518 | 0.3678        | <b>0.4025</b> |
|          | NDCG@5  | 0.1391 | 0.0934 | 0.1063  | 0.2268  | 0.2219 | 0.2656 | 0.2455    | 0.2353 | 0.2848        | 0.2622        | 0.2660 | <u>0.2864</u> | <b>0.3070</b> |
|          | HR@10   | 0.3386 | 0.2311 | 0.2872  | 0.4106  | 0.3942 | 0.4503 | 0.4205    | 0.4426 | 0.4696        | <u>0.4739</u> | 0.4484 | 0.4542        | <b>0.4998</b> |
|          | NDCG@10 | 0.1803 | 0.1207 | 0.1440  | 0.2584  | 0.2512 | 0.2965 | 0.2757    | 0.2715 | <u>0.3156</u> | 0.2975        | 0.2971 | 0.3143        | <b>0.3385</b> |
|          | MRR     | 0.1558 | 0.1096 | 0.1226  | 0.2308  | 0.2263 | 0.2669 | 0.2498    | 0.2376 | 0.2852        | 0.2614        | 0.2686 | <u>0.2882</u> | <b>0.3051</b> |
| Sports   | HR@1    | 0.0763 | 0.0489 | 0.0644  | 0.1160  | 0.1135 | 0.1428 | 0.1334    | 0.1114 | 0.1455        | 0.1255        | 0.1419 | <b>0.1669</b> | <u>0.1646</u> |
|          | HR@5    | 0.2293 | 0.1603 | 0.1982  | 0.3055  | 0.2866 | 0.3349 | 0.3162    | 0.3041 | 0.3466        | 0.3375        | 0.3367 | <u>0.3588</u> | <b>0.3803</b> |
|          | NDCG@5  | 0.1538 | 0.1048 | 0.1316  | 0.2126  | 0.2020 | 0.2420 | 0.2274    | 0.2096 | 0.2497        | 0.2341        | 0.2418 | <u>0.2658</u> | <b>0.2760</b> |
|          | HR@10   | 0.3423 | 0.2491 | 0.2967  | 0.4299  | 0.4014 | 0.4551 | 0.4324    | 0.4274 | 0.4622        | 0.4722        | 0.4545 | <u>0.4737</u> | <b>0.5059</b> |
|          | NDCG@10 | 0.1902 | 0.1334 | 0.1633  | 0.2527  | 0.2390 | 0.2806 | 0.2649    | 0.2493 | 0.2869        | 0.2775        | 0.2799 | <u>0.3029</u> | <b>0.3165</b> |
|          | MRR     | 0.1660 | 0.1202 | 0.1435  | 0.2191  | 0.2100 | 0.2469 | 0.2334    | 0.2156 | 0.2520        | 0.2378        | 0.2461 | <u>0.2691</u> | <b>0.2763</b> |
| Toys     | HR@1    | 0.0585 | 0.0257 | 0.0448  | 0.0997  | 0.1114 | 0.1504 | 0.1333    | 0.1104 | 0.1878        | 0.1262        | 0.1600 | <b>0.1996</b> | <u>0.1935</u> |
|          | HR@5    | 0.1977 | 0.0978 | 0.1471  | 0.2795  | 0.2614 | 0.3276 | 0.3001    | 0.3055 | <u>0.3682</u> | 0.3344        | 0.3389 | 0.3613        | <b>0.4063</b> |
|          | NDCG@5  | 0.1286 | 0.0614 | 0.0960  | 0.1919  | 0.1885 | 0.2423 | 0.2192    | 0.2102 | 0.2820        | 0.2327        | 0.2528 | <u>0.2836</u> | <b>0.3046</b> |
|          | HR@10   | 0.3008 | 0.1715 | 0.2369  | 0.3896  | 0.3540 | 0.4211 | 0.4015    | 0.4207 | <u>0.4663</u> | 0.4493        | 0.4413 | 0.4509        | <b>0.5062</b> |
|          | NDCG@10 | 0.1618 | 0.0850 | 0.1248  | 0.2274  | 0.2183 | 0.2724 | 0.2517    | 0.2473 | <u>0.3136</u> | 0.2698        | 0.2857 | 0.3125        | <b>0.3368</b> |
|          | MRR     | 0.1430 | 0.0819 | 0.1131  | 0.1973  | 0.1967 | 0.2454 | 0.2253    | 0.2138 | 0.2842        | 0.2338        | 0.2566 | <u>0.2871</u> | <b>0.3012</b> |
| Yelp     | HR@1    | 0.0801 | 0.0624 | 0.0731  | 0.2053  | 0.2188 | 0.2428 | 0.2341    | 0.2102 | 0.2375        | 0.2405        | 0.2176 | <u>0.2493</u> | <b>0.2727</b> |
|          | HR@5    | 0.2415 | 0.2036 | 0.2249  | 0.5437  | 0.5111 | 0.5768 | 0.5357    | 0.5707 | 0.5745        | <u>0.5976</u> | 0.5442 | 0.5725        | <b>0.6191</b> |
|          | NDCG@5  | 0.1622 | 0.1333 | 0.1501  | 0.3784  | 0.3696 | 0.4162 | 0.3894    | 0.3955 | 0.4113        | <u>0.4252</u> | 0.3860 | 0.4162        | <b>0.4527</b> |
|          | HR@10   | 0.3609 | 0.3153 | 0.3367  | 0.7265  | 0.6661 | 0.7411 | 0.6897    | 0.7473 | 0.7373        | <u>0.7597</u> | 0.7096 | 0.7371        | <b>0.7720</b> |
|          | NDCG@10 | 0.2007 | 0.1692 | 0.1860  | 0.4375  | 0.4198 | 0.4695 | 0.4393    | 0.4527 | 0.4642        | <u>0.4778</u> | 0.4395 | 0.4696        | <b>0.5024</b> |
|          | MRR     | 0.1740 | 0.1470 | 0.1616  | 0.3630  | 0.3595 | 0.3988 | 0.3769    | 0.3751 | 0.3927        | <u>0.4026</u> | 0.3711 | 0.4006        | <b>0.4299</b> |

# Experiments

**Table 5: Performance comparison of different methods on four session-based datasets. Since these datasets do not have attribute information and the item sequences are usually shorter, we remove several improper baseline methods.**

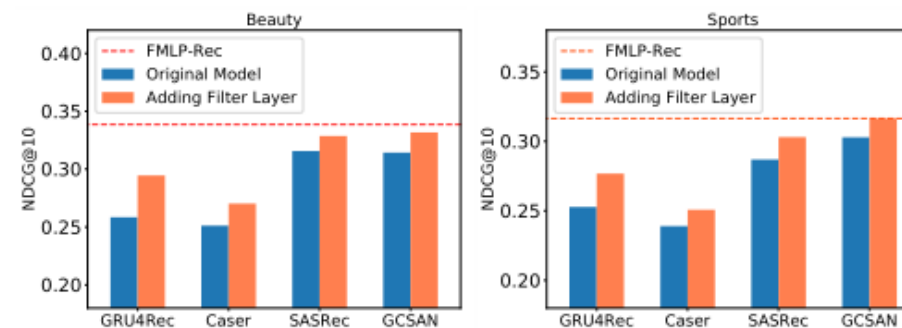
| Datasets     | Metric  | PopRec | GRU4Rec       | Caser  | HGN    | RepeatNet     | CLEA   | SASRec        | SRGNN  | GCSAN         | FMLP-Rec      |
|--------------|---------|--------|---------------|--------|--------|---------------|--------|---------------|--------|---------------|---------------|
| Nowplaying   | HR@1    | 0.0757 | 0.4035        | 0.3435 | 0.3491 | 0.3350        | 0.2728 | 0.4396        | 0.3819 | <u>0.4447</u> | <b>0.4731</b> |
|              | HR@5    | 0.2197 | 0.6829        | 0.6267 | 0.6026 | 0.5257        | 0.5575 | <u>0.7042</u> | 0.6028 | 0.6728        | <b>0.7262</b> |
|              | NDCG@5  | 0.1480 | 0.5536        | 0.4942 | 0.4835 | 0.4355        | 0.4226 | <u>0.5812</u> | 0.4986 | 0.5658        | <b>0.6094</b> |
|              | HR@10   | 0.3318 | 0.7720        | 0.7318 | 0.6992 | 0.6110        | 0.6766 | <u>0.7968</u> | 0.7007 | 0.7616        | <b>0.8081</b> |
|              | NDCG@10 | 0.1841 | 0.5825        | 0.5283 | 0.5149 | 0.4631        | 0.4612 | <u>0.6113</u> | 0.5304 | 0.5946        | <b>0.6360</b> |
|              | MRR     | 0.1602 | 0.5314        | 0.4752 | 0.4677 | 0.4297        | 0.4070 | <u>0.5615</u> | 0.4892 | 0.5520        | <b>0.5895</b> |
| Retailrocket | HR@1    | 0.0817 | 0.7202        | 0.6871 | 0.6432 | 0.6744        | 0.3410 | 0.7588        | 0.7408 | <b>0.7773</b> | <u>0.7736</u> |
|              | HR@5    | 0.2315 | 0.8597        | 0.8348 | 0.7650 | 0.7724        | 0.6139 | <u>0.8769</u> | 0.8373 | 0.8650        | <b>0.8810</b> |
|              | NDCG@5  | 0.1577 | 0.7982        | 0.7689 | 0.7098 | 0.7270        | 0.4853 | 0.8250        | 0.7937 | <u>0.8259</u> | <b>0.8338</b> |
|              | HR@10   | 0.3388 | 0.8925        | 0.8719 | 0.8036 | 0.8112        | 0.7296 | <u>0.9024</u> | 0.8684 | 0.8901        | <b>0.9060</b> |
|              | NDCG@10 | 0.1922 | 0.8089        | 0.7809 | 0.7223 | 0.7395        | 0.5227 | 0.8333        | 0.8037 | <u>0.8340</u> | <b>0.8419</b> |
|              | MRR     | 0.1694 | 0.7858        | 0.7563 | 0.7029 | 0.7234        | 0.4702 | 0.8145        | 0.7878 | <u>0.8199</u> | <b>0.8247</b> |
| Tmall        | HR@1    | 0.1025 | 0.4178        | 0.3288 | 0.4467 | <b>0.5556</b> | 0.2895 | 0.4045        | 0.4026 | 0.4650        | <u>0.5173</u> |
|              | HR@5    | 0.2264 | 0.5855        | 0.5066 | 0.5793 | <u>0.6090</u> | 0.4573 | 0.5478        | 0.5335 | 0.5940        | <b>0.6565</b> |
|              | NDCG@5  | 0.1647 | 0.5062        | 0.4230 | 0.5168 | <u>0.5826</u> | 0.3768 | 0.4792        | 0.4710 | 0.5329        | <b>0.5911</b> |
|              | HR@10   | 0.2967 | <u>0.6636</u> | 0.5943 | 0.6471 | 0.6494        | 0.5478 | 0.6275        | 0.6082 | 0.6591        | <b>0.7206</b> |
|              | NDCG@10 | 0.1874 | <u>0.5315</u> | 0.4513 | 0.5386 | <u>0.5956</u> | 0.4060 | 0.5049        | 0.4950 | 0.5538        | <b>0.6118</b> |
|              | MRR     | 0.1723 | 0.5021        | 0.4209 | 0.5168 | <b>0.5894</b> | 0.3775 | 0.4804        | 0.4736 | 0.5328        | <u>0.5879</u> |
| Yoochoose    | HR@1    | 0.1794 | 0.7208        | 0.7041 | 0.6278 | 0.7450        | 0.5106 | 0.7611        | 0.7575 | <b>0.7855</b> | <u>0.7749</u> |
|              | HR@5    | 0.4990 | 0.8950        | 0.8818 | 0.8425 | 0.8673        | 0.7628 | 0.8976        | 0.8840 | <u>0.9073</u> | <b>0.9084</b> |
|              | NDCG@5  | 0.3432 | 0.8189        | 0.8026 | 0.7460 | 0.8123        | 0.6465 | 0.8375        | 0.8280 | <b>0.8535</b> | <u>0.8499</u> |
|              | HR@10   | 0.6574 | 0.9273        | 0.9172 | 0.8927 | 0.9001        | 0.8436 | 0.9273        | 0.9137 | <u>0.9320</u> | <b>0.9359</b> |
|              | NDCG@10 | 0.3948 | 0.8294        | 0.8141 | 0.7623 | 0.8230        | 0.6727 | 0.8471        | 0.8376 | <b>0.8616</b> | <u>0.8588</u> |
|              | MRR     | 0.3276 | 0.8004        | 0.7838 | 0.7246 | 0.8019        | 0.6257 | 0.8240        | 0.8164 | <b>0.8414</b> | <u>0.8364</u> |



# Experiments

**Table 6: Ablation study of our FMLP-Rec, we report NDCG@10 on Beauty and Sports datasets.**

|                  | Beauty        |               | Sports        |               |
|------------------|---------------|---------------|---------------|---------------|
|                  | HR@10         | NDCG@10       | HR@10         | NDCG@10       |
| FMLP-Rec         | <b>0.4998</b> | <b>0.3385</b> | <b>0.5059</b> | <b>0.3165</b> |
| w/o Filter Layer | 0.4317        | 0.2914        | 0.4243        | 0.2604        |
| w/o FFN          | 0.4607        | 0.3067        | 0.4594        | 0.2838        |
| w/o Add & Norm   | 0.4654        | 0.2919        | 0.4831        | 0.2860        |
| +HPF             | 0.4567        | 0.3034        | 0.4595        | 0.2810        |
| +LPF             | 0.4847        | 0.3233        | 0.4949        | 0.3093        |
| +BSF             | 0.4822        | 0.3207        | 0.4835        | 0.2977        |



**Figure 3: Performance (NDCG@10) comparison of different models enhanced by our learnable filters.**



# Thanks